Education and the Income Differential: An Estimation for Rawalpindi City

KHALIL A. HAMDANI*

I. Introduction

Empirical tests of the human capital hypothesis—that education increases an individual’s income—have been undertaken in several countries with favourable results [13]. These results show that (1) income differentials between individuals of different educational levels are wide; (2) the differentials establish shortly after the initial years of work and maintain through the duration of the life cycle; (3) the differentials are greater in developing countries than in developed countries; (4) the returns to education, after allowing for educational costs, exceed the returns to physical capital investment in developing countries; (5) the highest returns are to primary education; and (6) private returns exceed social returns. Which, if not all, of these results are true for Pakistan is not known. This paper yields such comparative results through an application of the human capital hypothesis to Rawalpindi City. The data for Rawalpindi are for males and derive from a socio-economic survey conducted by the Pakistan Institute of Development Economics in 1975.

For the impatient reader, the unqualified results of the paper are as follows. The application of the human capital hypothesis to Rawalpindi City is favourable. For all surveyed males at all completed educational levels, income differentials emerge in the initial year of work and maintain over the life cycle. The differentials increase slightly by educational level: at the peak of the life cycle, the primary-educated earn only 1.1 times the earnings of the uneducated; while the secondary-educated earn 1.5 times the earnings of the primary-educated, and the college-educated earn 1.8 times the earnings of the secondary-educated. These ratios are low, though, in very rough comparison with those in other countries.

*The author is a Research Economist at the Pakistan Institute of Development Economics. Computations were performed by Abdul Wasay. Regressions were performed by Aqeel Ahmed. The author is grateful to Stephen E. Guisinger and Dennis N. De Tray for several specific suggestions and frequent discussion. The author is also grateful to Syed H.H. Naqavi for stylistic comments on an earlier draft of the paper.
The social returns to completed education vary between 8 and 13 percent. Although low, if allowance is made for productivity growth, then the returns are roughly compatible with the returns to physical capital investment. The private returns to completed education vary between 11 and 27 percent, and, generally, decline by educational level. For the lower educational levels, both social and private returns are slightly low in comparison with those in other countries. Finally, the excess of private returns over social returns is attributable to government educational expenditure, and the rise in the excess by educational level indicates that higher education is more heavily subsidized than lower education.

For the patient reader who desires the qualifications to these results, the organization of the paper is as follows. The next section broadly identifies the theoretical framework of the study. The subsequent section describes the various data utilized in the analysis, and specifically identifies the theoretical framework with a selection of variables and forms appropriate for the data. The fourth section estimates the earnings functions, derives the gross income differentials by age categories or age-income profiles, and calculates the marginal rates of return. The paper concludes with a summary of the results and a discussion of the policy implications.

II. Theoretical Framework

The human capital conceptualization of education is as an investment activity which yields a return over the lifetime of the educated individual [1]. There are several project analysis techniques to calculate this return and one of these is that of the internal rate of return: it is the discount rate which reduces to zero the present value of the lifetime income differentials attributable to education net of educational costs.\(^1\) As education is attained in stages, a separate rate, defined at the margin, is calculable for each educational level. The marginal rate, \(r\), is calculable by determining the following algebraic expression:

\[
\sum_{t} (Y_t - Y_{t-1}) (1 + r)^{-t} = 0
\]

where \(Y\) is net income and \((Y_t - Y_{t-1})\) is the net income differential attributable to the marginal educational level, \(e\), for each year, \(t\), of the individual’s lifetime. Clearly, the magnitude of the rate varies directly with the magnitude and timing of the net income differentials: the greater the differentials and the earlier these are realized, the higher is the rate of return.

The calculation of the net income differentials involves two major steps and numerous minor ones [13, Chap. 2]. The first major step is the estimation of the gross income differentials over the lifetime of the educated individual. The second major step is the derivation of the net income differentials through the deduction of educational costs. The numerous minor steps consist of corrections to either income or costs for such factors as differences in private and social perspective, noneducational determinants of income, and the probabilities

\(^1\)Note that there exists a debate on the correct choice of technique and that while the selection of the internal rate of return is most popular it is nonetheless arbitrary. See [13, p. 19].
of employment and life expectancy. The two major steps are now outlined in turn, while the minor steps are noted wherever appropriate.

The estimation by educational level of lifetime gross income differentials requires a separate estimation of an earnings function—a regression of income on age—for each educational level. The lifetime gross incomes to each educational level is then simply the difference between the estimated lifetime incomes for that level and the level preceding it. The lifetime gross incomes to each educational level are the social gains in increased productivity due to education (provided wages reflect the marginal product of labour), while the lifetime gross incomes calculated exclusive of income tax—by a regression of disposable income on age—are the private gains realized by the individual.

As individual lifetime longitudinal data are unavailable, the earnings function is fitted on cross-sectional data for employed individuals of varying ages at a given educational level. The presumption is that a cross-sectional age-income profile of an individual’s prospective educational peers determines the individual’s ex ante expectations of the returns to different educational levels.

For each educational level, a concave earnings function is estimated by a least squares regression of income on age, and on selected standardization variables. Notationally, the form of the regression is:

\[
\ln(Y) = a + bA - cA^2 + \sum d_i Z_i + u
\]

where \(\ln(Y)\) is the natural logarithm of income, A is age, and \(Z_i\) are standardization variables; of course, \(u\) is the well-behaved regression error, and the regression coefficients are \(a, b, c,\) and \(d_i\). The inclusion of the standardization variables correct for income differences between educational levels due to noneducational factors [13, pp. 28-9]. For instance, if the proportion of self-employed individuals declines by educational level, and if a part of self-employment income is likely to be a return to physical capital investment and not to education, then nonstandardization overestimates the age regression coefficients more for the lower educational levels than for the higher educational levels and, therefore, underestimates the income differentials attributable to education.

The standardization is attained by first allowing for such noneducational factors, \(Z_i\), in each educational level regression, and second by holding the \(Z_i\) constant in deriving each educational level’s age-income profile.

The derivation of the age-income profiles from the estimated earnings functions is straightforward. The profiles are simply plots of the standardized

---

2 Alternatively, an earnings function can be estimated for the pooled data of all educational levels. In this form, the earnings function is a regression of income on schooling and work experience; see [5]. This form is not considered necessary in the paper except for the postgraduate educational level for which very few observations necessitate a pooling with the college educational level.

3 If wages do not reflect the marginal product of labour, then corrections to gross incomes are necessary; see [13, p. 26]. Although there is a need for such corrections—the shadow wage of unskilled labour is estimated at one-half of the market wage [8]—no corrections are made in view of the absence of a similar estimate for skilled labour and of the lack of accurate information on the association of skill with educational level.

4 However, possible future shifts in the labour market are not considered, so that the calculated rates of return are not ideally ex ante; see [13, pp. 23-4]. It is possible to allow for simple productivity growth by the addition of the expected annual growth rate to the calculated rates of return; see [13, pp. 31]. Although there is reason to believe that expected productivity growth is positive [4, 7], the addition is not made in view of the present absence of an accurate estimate.
regressions in an age-income Cartesian plane; as such, each depicts the lifetime expected incomes for a particular educational level. Theory suggests that each profile follows the life cycle: it rises initially with age through the accumulation of job experience, peaks at middle age, and then gradually declines with increased age.\footnote{The decline is more rapid for profiles derived from cross-sectional data due to the 'vintage effect': individuals are not homogeneous in the quality of their education as new technology is embodied in younger individuals\cite[p. 143]{Hamdan}.} Theory also suggests that the profiles for higher educational levels rise above those for lower educational levels—once the inexperience handicap resulting from a delayed entry into the job market is overcome—so that income differentials emerge and maintain over the life cycle. Clearly, whether these differentials yield high rates of return depends on educational costs.

Educational costs are of two types: monetary and opportunity. Monetary costs comprise all direct and indirect expenditures on education. The former include the cost of tuition, books, supplies, and teacher salaries (not paid from tuition revenue); the latter include the capital cost of classroom building and other school property (also not paid from tuition revenue). Opportunity costs value the time allocated to education and comprise all earnings foregone during school attendance.\footnote{Note that for primary education the age of job entry determines the commencement of foregone earnings but that the valuation of time allocated to schooling may still be positive (for instance, due to at-home productivity), in which case opportunity costs are underestimated and the returns to primary education are overestimated.} Although nonmonetary, foregone earnings for the relevant time period derive readily from the age-income profile of the $Y_{e-1}$ educational level, which represents the highest income alternative to school attendance.

The distinction between private and social costs is simple. Private cost is that incurred by the individual. This consists of the individual’s monetary expenditures on tuition (less any financial assistance provided to the individual), books, supplies, and the opportunity cost of foregone earnings, all expressed annually for each year of school attendance. Social cost is that incurred by society. This consists of the private cost and all remaining expenditures not incurred by the individual such as the cost of teacher salaries and school property (not paid from tuition revenue), also expressed annually per pupil.

Finally, the deduction of annual private (social) costs from the estimated annual private (social) gross income differentials yields, for each educational level, the lifetime private (social) net income differentials. As the net incomes derive from earnings functions estimated for employed individuals (who by definition are alive), corrections for the probabilities of employment, $w$, and life expectancy, $s$, are necessary as these effects are not reflected in the estimations.\footnote{A correction is sometimes made for the probability of labour force participation on the assumption that the labour force entry decision, like the employment and life expectancy decisions, is also determined exogenously and not by the individual. This assumption is not made in the paper and no labour force participation correction is considered.} The corrections imply a downward adjustment to the lifetime net income differentials. Notationally, the adjusted differentials for each educational level, $e$, are:

$$\Sigma w_t s_t (Y_e - Y_{e-1})_t$$

where both $w$ and $s$ are positive but less than unity, and are indexed by $t$ as these vary over the life cycle. The discount rate which reduces to zero the present...
value of these adjusted differentials is the rate of return to the marginal educational level, e.

The probability rates $w_t$ and $s_t$ are defined as follows. The employment rate, $w_t$, is the proportion of employed individuals in the labour force of age $t$. And the life expectancy rate, $s_t$, is the proportion of individuals alive at the initial school-going age (of the particular educational level) who survive to the year $t$. Ideally, these rates should be calculated separately for each educational level. This disaggregation is especially appropriate for $w_t$ as the probability of employment is likely to vary (and not necessarily positively) with educational attainment.

III. Data

Two principal types of data are used in the paper. The socio-economic data are from a 1,000-household survey of Rawalpindi City. The educational cost data are from national estimates by the Government of Pakistan. Both data are for 1975. The survey data are discussed first.

A. Socio-Economic Data

To begin with, some brief characteristics of Rawalpindi City are useful. The most important of these is that Rawalpindi is the fifth largest Pakistani city with an estimated population of 673,000 individuals in 1975. The city is an important regional metropolis, with primarily administrative functions. In the early Sixties, it was the nation's interim capital. Even today, several of the earlier capital functions remain. With the development of Islamabad, the new capital on its outskirts, Rawalpindi's wholesale trade and construction activities expanded, and have emerged as important. However, manufacturing activity is largely nonexistent in the city.

In August and September of 1975, the Pakistan Institute of Development Economics undertook a socio-economic survey of 1,000 Rawalpindi households. A tight budget necessitated the small sample size and a simple sampling design. A discussion of the sampling design and possible sampling and nonsampling errors is presented in the Appendix. The discussion indicates that the sampled households are representative of Rawalpindi. And, it concludes that the methodology of the previous section is appropriate if applied to the male subsample.

The summary statistics for the data of interest are as follows. There are 1,664 individuals in the labour force, of whom 1,541 are males. Half the males in the labour force, 50.4 percent, are employees, while 33.7 percent are self-employed; almost all of the former, 97.7 percent, are salaried, and almost all of the latter, 88.5 percent, are individual operators. Surprisingly, only 5.3 percent of the males in the labour force are unemployed; underemployment, though, is substantial: 23.8 percent of the males would like to work more hours. The minority members of the labour force are apprentices, 3.2 percent, and unpaid family helpers, 7.5 percent.

---

8The estimation is a projection of the 1972 Census estimate at a 3.2 percent annual growth rate.
9It notes, though, the possibility of an underestimation of the return to primary education due to the sampling of only structured and semi-structured dwellings.
10This is, however, an unsatisfactory measure of underemployment.
The subsample of all employed and self-employed males is chosen for analysis. Apprentices are excluded for a theoretical reason: although in the labour force, they are also investing in human capital through on-the-job training so their earnings are lower (by the amount of the trainee cost) than the earnings of nonapprentices, and the two earnings are not comparable, therefore [1, p. 15]. It is possible to include the unemployed and so directly correct the income differentials for the probability of employment [13, p. 29], this is not done, however, as the unemployment rate yielded by the sample, 5.3 percent, appears to be low; instead, the indirect employment correction indicated in the previous section is used. Ideally, unpaid family helpers should be included; they are excluded, though, because their income is not easily determinable. Still, it is possible to allow for their presence indirectly: a standardization variable indicating the number of unpaid family helpers associated with each self-employed individual—the variable is necessarily zero for employees—is defined for the earnings functions.

Analysis of the self-employed is troublesome because a portion of self-employment income tends to be a return to physical capital investment. A reasonable assumption is that the return is low for individual operators (who presumably own little capital stock) and high for those self-employed with employees. If correct, then the problem is serious for only a fraction, 4.6 percent, of the selected subsample. Again, an appropriate allowance for the problem is possible. A standardization variable, this time a dummy (=1 if an individual is self-employed with employees, and 0 otherwise), is defined for the earnings functions.

The distribution of the selected subsample of 1,295 individuals by educational level is as follows.11 Four hundred and thirty-nine are unschooled of whom 50 are functional literates; 119 have less than primary schooling. Two hundred and eighty-five have completed primary school and possibly some secondary schooling; 375 have completed secondary school through matriculation and possibly some college education. Sixty-seven have completed college and received a B.A. degree; and 10 have attended university and received a post-graduate degree. This arbitrary, discontinuous grouping is unfortunate; yet, it is the response grouping of the educational question used in the survey.

With one exception, the above distribution yields sufficient observations per educational level group to allow the estimation of a separate earnings function for each. The exception is the university educational level which, for the estimation purpose, is combined with the college educational level to form a post-secondary group of 77 observations. For the latter group, a dummy variable (=1 for university graduates and 0 otherwise) is defined to distinguish between the age-income profiles of the college and university educational levels. This technique assumes that the two profiles are similarly shaped and differ only in the intercept. Although perhaps an acceptable assumption, any interpretation of the dummy variable coefficient must be cautious as its estimation depends on only 10 observations.

11Education in Pakistan consists of: 5 years of primary school; 3 years of middle school and 2 years of high school, both of which together comprise secondary school and completion of which is termed matriculation; 2 years of intermediate college and 2 years of degree college, both of which together comprise college and the completion of which is marked with the award of a B.A. degree; and 2 years of university, the completion of which is marked with the award of a post-graduate degree. As a simplification, medicine, engineering, and similar specialized education are not considered.
Income, the dependent variable in the earnings functions, is defined as hourly earnings. Specifically, it is the ratio of monthly income to monthly hours worked, where monthly income is wage income (including bonus payments) and income in kind for both primary and secondary occupations, and monthly hours worked are the hours worked in the survey reference week multiplied by 4. The choice of hourly earnings is based on observed variations in the sample in the average hours worked per week between individuals of different educational levels: the educated tend to work fewer hours than the uneducated. As noted in the Appendix, these variations in part may be due to nonsampling error (since the uneducated are proportionately more self-employed); however, in part these also reflect an individual’s time allocation decision between work and leisure. In the latter and potentially more important case, hourly earnings standardize for this substitution effect and are, therefore, a more appropriate measure of income.\(^\text{12}\)

It is desirable to conclude this discussion of the survey data with a review of the calculations to be performed in the next section. For each of five educational level groups [unschooled, incomplete primary, primary (-plus), secondary (-plus), and post-secondary], consisting of employed and self-employed males, an earnings function is estimated by a regression of the natural logarithm of hourly earnings on age and two standardization variables. Also, the earnings function estimation for the post-secondary educational level group includes a dummy variable identifying university graduates in order to derive an age-income profile for these individuals, and the estimation for the unschooled group includes a dummy variable for functional literates.\(^\text{13}\) The two standardization variables attempt to control the effects of unpaid family helpers and nonearnings income. The standardization is attained in two ways: first, within each educational level’s earnings function, by an evaluation of the function with these variables set to zero (since all calculations are for individuals with no unpaid family helpers and no nonearning income); and second, between educational levels, by maintaining these variables constant at zero in the derivation of each educational level’s age-income profile.

B. Cost Data

The initial step in the specification of costs is to determine the number of years of schooling associated with each educational level. The determination is simple for the unschooled, college, and university levels: at 0, 4, and 2 years of marginal schooling, respectively; however, the determination is approximate for the three open-ended educational level groups; incomplete primary, primary (-plus), and secondary (-plus). The years of schooling for the incomplete primary group is determined at 2 [which is the average number of years of incomplete primary schooling \(= (5-1)/2\)]. The average years of schooling of the primary (-plus) group and the marginal years of schooling of the secondary (-plus) group are determined at 5 each on the simple assumption that the proportion who complete further years is small so that the distribution of individuals is skewed towards 5 years of (average or marginal) schooling; if the latter assumption is incorrect, then its effect—if any—is to over-estimate the

\(^{12}\)Even in the former case, standardization may be appropriate as nonwork time incurred in underemployment is not strictly leisure.

\(^{13}\)No age-income profile is derived for functional literates, though.
return to primary and secondary education.\textsuperscript{14} Note that the above determination does not consider—due to lack of data—the likelihood of individuals repeating one or more years of schooling.

The next step is to determine the annual cost of schooling. As already noted, the cost consists of all monetary expenditures on schooling and all earnings foregone during school attendance. The latter derive readily from the age-income profile of the $Y_{e-1}$ educational level. The former ordinarily derive from expenditure data, but unfortunately none exist; instead, these derive from national estimates by the Planning Commission [12], and the Bureau of Educational Planning [11]. The expenditure estimates are detailed in Appendix Table 1; although perhaps slightly low, no attempt to second guess is made.

The average annual cost of schooling by educational level is summarized in Table 1. Two rough comparisons of these figures with those for other countries are possible. First, as in most countries, opportunity cost (=private total cost—private direct cost) is the principal component of social cost for primary and secondary education; however, the proportions 60 and 72 percent are high relative to those observed in developing countries, 46 percent and 53 percent [13, p. 177]. Second, ignoring opportunity cost and all indirect costs, the direct cost of a year of secondary (college) education is twice (nine times) the cost of a year of primary education; these cost ratios are identical to those observed in developed countries but much less than those in developing countries, 7:1 (and 77:1), [13, p. 127]. In view of these disparities it is important to emphasize that the expenditure cost data for Pakistan derives from estimates.

<table>
<thead>
<tr>
<th>Educational Level</th>
<th>Years of Schooling</th>
<th>Social Cost</th>
<th>Government Cost</th>
<th>Private Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Total</td>
<td>Direct (%)</td>
<td>Total</td>
<td>Direct (%)</td>
</tr>
<tr>
<td>School</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Primary</td>
<td>5</td>
<td>694</td>
<td>246</td>
<td>59</td>
</tr>
<tr>
<td>Middle</td>
<td>3</td>
<td>2,123</td>
<td>507</td>
<td>59</td>
</tr>
<tr>
<td>High</td>
<td>2</td>
<td>2,524</td>
<td>710</td>
<td>56</td>
</tr>
<tr>
<td>College</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intermediate</td>
<td>2</td>
<td>4,742</td>
<td>1,931</td>
<td>52</td>
</tr>
<tr>
<td>Degree</td>
<td>2</td>
<td>5,574</td>
<td>2,441</td>
<td>49</td>
</tr>
<tr>
<td>University</td>
<td>2</td>
<td>21,985</td>
<td>17,414</td>
<td>29</td>
</tr>
</tbody>
</table>

Source: Appendix Table 1 and age-income profiles (for opportunity cost).
Note: Annual opportunity cost is calculated for a ten-month schooling cycle.

IV. Analysis

A. Earnings Functions

For each educational level, an earnings function is estimated as specified in the previous section; the estimations are summarized in Table 2. By standard

\textsuperscript{14}Given the assumption, the (plus) qualification is deleted from the primary and secondary educational level groups.
### Table 2

**Male Earnings Functions by Educational Level**

<table>
<thead>
<tr>
<th>Educational Level</th>
<th>Sample Size</th>
<th>Regression Coefficients (t-statistic value)</th>
<th>ln(Y)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Constant</td>
<td>Age</td>
</tr>
<tr>
<td>Unschooled</td>
<td>439</td>
<td>—1.1410</td>
<td>0.0684</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(9.20)</td>
</tr>
<tr>
<td>Incomplete Primary</td>
<td>119</td>
<td>—1.3744</td>
<td>0.0800</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(5.83)</td>
</tr>
<tr>
<td>Primary</td>
<td>285</td>
<td>—0.7955</td>
<td>0.0615</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(5.49)</td>
</tr>
<tr>
<td>Secondary</td>
<td>375</td>
<td>—1.0190</td>
<td>0.0962</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(7.97)</td>
</tr>
<tr>
<td>Post-Secondary</td>
<td>77</td>
<td>—1.1389</td>
<td>0.1166</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(2.89)</td>
</tr>
</tbody>
</table>

**Note:** The dependent variable, ln(Y), is the logarithm of before-tax hourly Rupee earnings.
criteria, the estimations are good. All equations are significant at the 1 percent level, by the F-test. The human capital variables in all equations possess expected signs and are also significant at the 1 percent level, by the t-test. And, the goodness-of-fit of all regressions—the $R^2$ varies between 20 percent and 43 percent—is respectable for household data if it is recalled that the samples are stratified by education (itself a principal determinant of income and the dependent variable is hourly earnings instead of monthly earnings).

The importance of the standardization and dummy variables varies. The helpers variable, a standardization for unpaid family helpers, and the employer variable, a standardization for nonearnings income, are important only for the lower educational levels. This is traceable to occupational differences between educational levels: the more educated tend to enter employee occupations rather than self-employment occupations. The literate variable, a dummy identifying the literate among the unschooled group, is insignificant suggesting no wage premium for functional literacy. However, the university variable, a dummy identifying university graduates among the post-secondary group, is positive and significant at the 5 percent level, by the t-test.

A cursory look at the variance of the dependent variable provides a rough indication of the differences in income inequality between educational levels. The variance of $\ln(Y)$ is a popular measure of income inequality [2, p. 7]. By this measure, income inequality is the greatest among the unschooled, and it is the least among the primary-schooled. Generally, the degree of income inequality declines by educational level, if allowance is made for the heterogeneous nature of the post-secondary educational level. Note, though, that the decline could reflect differences in income dispersion between educational levels due to noneducational factors.

A similar look at the mean of the dependent variable provides an indication of the differences in income between educational levels. The mean of $\ln(Y)$ is the logarithm of the geometric mean of $Y$, and is therefore a popular central tendency measure of income [2, p. 7]. By this measure, hourly earnings rise by educational level. The marginal rises for the secondary and post-secondary educational levels are significant at the 1 percent level, by t-tests of the difference between means modified for unequal variances. However, the rises for the lower educational levels are insignificant.

B. Age-Income Profiles

The differences in income between educational levels are more appropriately viewed over the life cycle. Figure 1 presents age-income profiles, derived from the earnings functions in Table 2, for all educational levels.\footnote{The college (university) profile is derived from the post-secondary earnings function with the university variable set at 0 (1). For all profiles, the derivation procedure is as follows. First, the standardization and literacy variables are set at 0. Second, estimated hourly earnings are calculated for all regressions for an assumed 65-year life cycle. The initial years vary depending on the age of job entry. The latter is set at 8 years—the age of the youngest worker in the sample—for the unschooled group and at 5 plus the number of years of schooling—the age immediately following the age of school completion—for the remaining groups. Third, the estimated hourly earnings are converted to annual earnings; to do so, $2,304 (=48 \times 4 \times 12)$ hours of work in a year are assumed. Finally, the annual earnings are plotted in ten-year age intervals in an age-income Cartesian plane, and the plots are connected with linear line segments. Note that the profiles appear to peak at the same age since the actual peaks lie in the same age interval. In fact, the average peak age is 49 years, and the peak age range is 45 to 53 years.}
Figure 1
Male Age-Earnings Profiles by Educational Level
As expected, the profiles are concave and follow the life cycle: these rise initially with age through the accumulation of job experience, peak on the average at age 49, and then decline with increased age. With one exception, the concavity of the profiles increases by educational level. Also with one exception, the profiles for higher educational levels are above those for lower educational levels so that income differentials emerge with the initial year of work and maintain over the life cycle.

The latter exception is the profile of the incomplete primary educational level. Although below the unschooled profile initially, it rises above the unschooled profile (at about age 20), the primary profile (at about age 40), and the secondary profile (at about age 60). The initial negative income differential is intuitively a puzzle: presumably, individuals do not complete school due to high opportunity costs; yet, the earnings of those who do leave school are lower than the earnings of those who do not attend school. One explanation is on-the-job training [1, p. 15]: the initial negative differential could represent an implicit training investment cost, and the subsequent, increasingly positive income differential would then represent a joint return to the training and the partial schooling. An alternate explanation is the 'screening hypothesis' [9, p. 986]: in the absence of a certification of incomplete schooling, school leavers are initially underpaid their marginal product.

Returning to the differences in income between educational levels, these increase by educational level, but slightly. The ratios of gross annual income differentials at age 49 for primary/unschooled, secondary/primary, and college/secondary are 1.12, 1.47, and 1.84, respectively. The college-educated earn three times the earnings of the uneducated. These ratios are low in very rough comparison to those for other developing countries (where the average secondary/primary ratio is 2.39), and are in line with those in developed countries (where the average secondary/primary ratio is 1.43). The low magnitude of the ratios is partly explained by the urban setting of the earners sample, though.

C. Rates of Return

The analysis now turns to the net differences in income between educational levels. As indicated in the second section, the project analysis technique selected to relate income benefits with costs is the internal rate of return. Table 3 presents the private and social internal rates of return to all (marginal) educational levels. The calculation of the social rates is based on the before-tax, age-income profiles in Figure 1 and on the social cost estimations in Table 1; while the calculation of the private rates is based on after-tax, age-income...

\[\text{\footnotesize {Ole D.K. Norbye suggests that the peak may be exaggerated due to the possibility of a 'partition effect': individuals at age 49 in 1975 were at age 21 in 1947, the year of the partition of the sub-continent, and were therefore in a position to rapidly advance their careers in the initial years of Pakistan's formation.}}\]

\[\text{\footnotesize {Recall, though, that apprentices are excluded from the sample so the explanation presumes nonformal on-the-job training. And further note that the explanation presumes that the effect is more pronounced relative to other educational levels.}}\]

\[\text{\footnotesize {The comparison is very rough as the ratios and educational levels for other countries are computed differently; see [13, p. 132].}}\]
profiles (not presented) and on the private cost estimations in Table 1. All rates are corrected for the probability of life expectancy.19

For all educational levels, private returns exceed social returns. Ignoring the extreme levels, the excess is 2-7 percentage points. Between educational levels, the variation in private returns exceeds the variation in social returns. Private returns vary between 7 and 27 percent, while social returns vary between 5 and 13 percent, only. Generally, both private and social returns decline by educational level, again ignoring the extreme levels.

Table 3

Marginal Rates of Return to Education by Level

<table>
<thead>
<tr>
<th>Educational level</th>
<th>Years of Schooling</th>
<th>Returns (in percentage)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Private</td>
</tr>
<tr>
<td>Incomplete Primary</td>
<td>2</td>
<td>7</td>
</tr>
<tr>
<td>Primary</td>
<td>5</td>
<td>20</td>
</tr>
<tr>
<td>Secondary</td>
<td>5</td>
<td>11</td>
</tr>
<tr>
<td>College</td>
<td>4</td>
<td>14</td>
</tr>
<tr>
<td>University</td>
<td>2</td>
<td>27</td>
</tr>
</tbody>
</table>

Note: The returns to the primary level are marginal with respect to the unschooled level and not the incomplete primary level, and are therefore average returns. All rates are corrected for the probability of life expectancy.

In comparison with other countries, the returns to primary and secondary education are slightly low.20 For both primary and secondary education, private and social returns are about 5 percentage points below the averages of comparable returns in other countries but are inside the standard deviations of the averages. These differences are acceptable, given the imprecision of the comparison. For the primary, secondary, and college levels, the rates exhibit the general pattern observed in other countries of declining returns by educational levels. And, the 2-7 percentage point excess of private returns over social returns is comparable with a 3-6 percentage point excess observed in other countries.

The absence of reliable employment rate estimates prevents the calculation of returns corrected for the probability of employment. However, a common presumption is that unemployment is serious primarily for individuals with secondary and post-secondary education and, also primarily for their initial years in the job market due to the inexperience handicap resulting from their delayed entry.21 If true, then a check on the sensitivity of returns to the probability of employment is possible with the use of arbitrary but reasonable correction rates. If it is assumed that the probabilities of employment in the first five years of entry in the job market for individuals with secondary and post-secondary education are, respectively, .50, .75, .85, .90, and

19 The probability of life expectancy, \( s_t \), for each year \( t \) of the life cycle is calculated as the multiplicative product of the survival rates for all years between the initial school-going age (of a particular educational level) and the age \( t \). The survival rates are from [3, Appendix Table 1B].

20 All comparisons with other countries are based on figures in [13, Chap. 4].

21 By this presumption, the age-income profiles for higher educational levels in Figure 1 might initially lie below those for lower educational levels if the profiles were corrected for the probability of employment.
.95, then the corrected social returns to secondary, college, and university education are 9 percent, 9 percent, and 7 percent, respectively. And, the corrected private returns are 11 percent, 13 percent, and 26 percent, respectively.

Evidently, returns are relatively insensitive. The employment correction lowers the returns by not more than a percentage point. This result is similar to that observed in other countries [6, p. 23]. On the matter of sensitivity, rates of return were also calculated without the life expectancy correction, and for nonstandardized earnings functions. These rates do not differ from those presented in Table 3, except for the incomplete primary level and, then too, the differential is only 2 percentage points.

The returns to primary education, though, are sensitive to alternate assumptions of the commencement of opportunity costs. If instead of the observed sample age of job entry, 8 years, progressively lower ages of years 7, 6, and 5, are assumed to allow for at-home productivity, then private (social) returns decline to 14 (10) percent, 10 (8) percent, and 9 (7) percent, respectively. This decline is not unexpected: recall that average annual opportunity costs are 93 (60) percent of average annual private (social) costs and that opportunity costs rise with a lowering of the age of job entry. However, these alternate returns calculations are only indicative and are not precise as the variance associated with the estimated opportunity cost values is likely high since these derive from beyond the estimation range of the earnings function, and moreover, as the costs do not fall rapidly, as is expected—this is the case even with the use of a linearly segmented earnings function. For these reasons, and because the use of the observed sample age of job entry is standard procedure, the procedure is retained; nonetheless, these very rough calculations suggest the sensitivity of returns to at-home productivity assumptions which should be noted when returns are used to indicate the private incentives in favour of primary education.

V. Conclusion

The results of the paper are summarized as follows. For all completed educational levels, income differentials emerge with the initial year of work and maintain over the life cycle. The differentials increase slightly by educational level: at the peak of the life cycle, the primary-educated earn only 1.1 times the earnings of the uneducated; while the secondary-educated earn 1.5 times the earnings of the primary-educated, and the college-educated earn 1.8 times the earnings of the secondary-educated. These ratios are low, though, in very rough comparison with those in other countries. Differentials are not observable for functional literates, and the differentials observable for the incomplete primary-educated are apparently influenced over the life cycle by either on-the-job training or the so-called 'certificate effect'.

The social returns to education vary between 5 and 13 percent; however, the returns to completed education vary only slightly, between 8 and 13 percent. The private returns to education vary between 7 and 27 percent, and, generally, decline by educational level. The private return to primary education is 20 percent, while the private return to secondary education is 11 percent. For the lower educational levels, both social and private returns are slightly low in comparison with those in other countries. Finally, there is incidental indication that the degree of income inequality declines by educational level.
The above results are subject to five specific and four broad qualifications. The specifics: first, the rates reflect returns to male education in an urban environment—Rawalpindi City; at best, therefore, the returns are representative for males in other urban areas, in no case are these representative for females or rural areas. Second, even for Rawalpindi the sample is small, so all inferences from the results—especially those for the sparsely represented higher educational levels—should be guarded. Third, the cost data are derived from estimates. Fourth, the returns are uncorrected for unemployment, but these appear to be insensitive to such a correction; and fifth, the returns do not allow for productivity growth over time—if the annual rate of growth is known, though, it should be added to the returns.

Now the broader qualifications: first, the returns assume that market wages reflect the marginal product of labour; if incorrect, then the sensitivity of the returns to different reflection patterns should be explored. Second, while the earnings functions standardize for non-earnings income, unpaid family helpers, and weekly hours worked, the functions do not standardize—due to lack of data—for family background and ability. For the latter, a popular alternative to standardization is an arbitrary downward correction to age-income profiles [13, p. 28]; no such correction is attempted. Third, also due to lack of data, no allowance for the wastage cost of school repeaters or dropouts is possible. Finally, the net consumption benefits of education are ignored in the calculations, so such benefits should be regarded as additional to the calculated returns.

Given these qualifications, the policy implications of the results can be assessed. The first concerns the investment choice between human capital and physical capital. Generally, the social returns to education are low. However, for the investment allocation decision it is especially important to allow for labour productivity growth: if allowance is made, for instance, for a 2 percent annual growth in productivity, then the social returns to completed education rise to 10-15 percent, and these are comparable with a 12-15 percent return to physical capital investment [8, p. 406]. With an allowance for productivity growth, therefore, investment in education is about as profitable as investment in physical capital.22

The second policy implication concerns the investment choice between educational levels. The social return to primary education is higher than the social returns to other educational levels. However, the differential in social returns is too narrow to recommend resource allocation towards any particular educational level. Rather—unless the consumption benefits of education are strongly skewed—the recommendation is for investment at all levels of education.

The third policy implication concerns the difference between social and private returns to education. Private returns exceed social returns and the excess rises by educational level from 2 percentage points to 19 percentage points. As the excess is attributable to government educational expenditure (and only negligibly to the income tax adjustment), the rise in the excess by educational level indicates that higher education is more heavily subsidized.

22The reader can modify this statement to suit different figures if the above are unreasonable.
than lower education. Evidently, this distribution reflects government policy. In any case, the present policy of free primary and secondary education provides only a small subsidy—a 2-7 percentage point excess differential in returns—relative to the existing college and university education subsidy—a 4-19 percentage point excess differential in returns.

The fourth policy implication concerns the wide variation—of 20 percentage points—in the private returns to education. The variation is largely at the extreme educational levels: the return to incomplete primary education is one-half of the returns to primary, secondary, and college education; while the return to university education is almost double the returns to primary, secondary, and college education. Such wide variations indicate a highly imperfect market; the low return to incomplete primary education suggests an excess supply of individuals at that level and, or, the operation of a ‘certificate effect’; while the high return to university education suggests a shortage of individuals at that level. Although such a market situation ranks private incentives in favour of further education, only individuals from relatively high income families with access to low-cost educational financing can realize the high returns on further education. Even then, the demand for higher education could exert excessive market pressure on existing higher educational facilities—pressure which does not reflect social resource allocation considerations.

A narrowing of the private returns is recommended, therefore. This is possible with a shift in the finance of university direct costs from the government to the private sector. A 1,000-rupee increase in the annual university student tuition lowers the private return to university education from 27 percent to 23 percent or by only 4 percentage points; a further 1,000-rupee increase lowers the return by only an additional 3 points; and an even further 1,000-rupee increase lowers the return by only an additional 2 points. In fact, a complete shift in the finance of university direct costs to the private sector is possible without altering the ranking of private incentives in favour of university education: a 5,000-rupee increase in the annual university student tuition lowers the private return to university education to 15 percent—which is still the highest return to any post-primary educational level. To ensure that a tuition increase does not deprive individuals from low income families of a university education, appropriate low-cost educational finance schemes can be established through existing credit institutions.

The fifth policy implication concerns the government policy to universalize primary education. The results of the paper are too limited in scope to

---

23Such a policy was stated by the Federal Minister for Education, Abdul Hafeez Pirzada, in a speech delivered at the Installation and Oath Taking Ceremony of the Students Union of the Quaid-i-Azam University, Islamabad, on October 26, 1976.

24The argument assumes imperfect access to educational financing. If this argument is too intuitive, the reader is referred to formal models of the private demand for education from which the argument derives; see [13, pp. 77-79] for a discussion and references.

25Although unsubstantiated in the paper, the assessment that the private demand for higher education presently exceeds the capacity of existing facilities is reasonable.

26The cautious reader may prefer a lower tuition increase than 5,000 rupees, however; not only because a large increase is impractical, but also because a safe margin of error should be attached to the university income differentials as these are based on few data observations. In defence of the estimations, though, a careful scrutiny of the university age-income profile in Figure 1 shows it to be very realistic, if not low, in comparison to the National Pay Scale for government employees with an M.A. degree who typically commence work at the Grade 16 level.
substantiate the desirability of this policy. Perhaps no analysis which ignores the consumption benefits of literacy should even attempt to do so. However, if the policy is accepted as given, then it is useful to note that any shift in the finance of university direct costs from the government to the private sector releases funds which can be allocated toward primary education. A quick calculation shows that a 1,000-rupee increase in the annual university student tuition allows an approximate 1 percent increase in national primary school enrolment.27

The sixth policy implication concerns the opportunity cost of primary education. The survey data indicate a relatively high opportunity cost to the final years of primary education: for these years, opportunity cost comprises 97 (79) percent of total private (social) cost. Since the years cover ages 8-9, the cost is frequently de-emphasized: the labour force entry age is typically assumed at 10, for instance; however, such de-emphasis is misleading. Opportunity cost is both apparent and real, and needs to be recognized if the private incentives in favour of primary education are to be improved. A corollary to this implication is that a further reduction in direct cost will yield a negligible improvement in the private incentives in favour of primary education.

The final policy implication is speculative and concerns the potential benefit of primary curricular reform. A proposal presently debated is the institution of an intensive learning programme designed to shorten the primary years of schooling to 4 years.28 If it is assumed that such a programme alters the duration of education with no sacrifice in quality, then the effect of a four-year schooling programme is to raise the private return to primary education by 6 percentage points to 26 percent, and to raise the social return by 4 percentage points to 18 percent.29 It is important to emphasize that these rises are speculative as a static labour market is assumed. Still, these are sufficiently encouraging to recommend a careful analysis of the proposal.

27The calculation: (1,000) (13,000)/(246) (5,093,430) = .01 where 13,000 (5,093,430) is national university (primary) enrolment for 1975 [12, Chap. 22], and 246 is the annual per student rupee cost of primary education incurred by the government.
28Such a programme has been established in Nepal and is under consideration in other countries. In Pakistan, a principal proponent is Khalid H. Bokhari of the Ministry of Education’s Bureau of Educational Planning.
29Note that the rises are attributable largely to a reduction in opportunity cost so if direct cost is to increase, which is likely, the rises would still be about the same magnitude.
The PIDE Socio-Economic Survey, Rawalpindi, 1975

In August and September of 1975, the Pakistan Institute of Development Economics undertook a socio-economic survey of 1,000 Rawalpindi households. A tight budget necessitated the small sample size and a simple sampling design. The latter involved, first, a random selection without replacement of 16 clusters—a cluster consists of approximately 255 households—from a 400-cluster sampling frame developed for Rawalpindi City by the Central Statistical Division. And second, a selection of a fixed proportion of households per cluster, \( x (=1,000/16) \), from the Division’s cluster-wise address listing of all structured and semi-structured dwellings. The household selection criterion was to sample every \( ith \) (= the total number of dwellings/x) address, given a randomly chosen initial address.

Basic socio-economic information was collected for each of the 1,000 selected households. For this purpose, a 57-item questionnaire was developed, twice pre-tested, and revised. The revised questionnaire was completed for each household by one of six direct-hire professional enumerators through an interview with the head of household or, if unavailable, the seniormost household member. Interviews were conducted on Sundays and weekday evenings to minimize the probability of unattended dwellings. All completed questionnaires were field checked by a supervisor at the close of each enumeration day for omissions and ambiguous answers; if necessary, the enumerators were instructed to re-conduct unsatisfactory interviews.

Two types of sampling error can arise for the above sample size and design. First, small samples generally yield few observations for minority groups so generalization derived from the data for these groups could be erroneous. As expected, the sample yielded 1,541 males and only 123 females in the labour force. Even the male subsample, when disaggregated by educational level, yields few observations for the higher educational levels: only 10 males have university education. To avoid possible errors associated with inadequate sample size, the paper analyses only the male subsample and, moreover, focuses attention on only the lower educational levels.

Second, small, simply selected samples are generally unrepresentative of the larger population, so any generalization derived from the data could be erroneous. One technique which reduces the possibility of this type of sampling error is stratification. Although the sampling design does not allow for stratification, a post-selection examination indicates that the selected clusters are geographically well-stratified. Within clusters, however, the sampling of only structured and semi-structured dwellings introduces the possibility of skewed income, educational, and migrant status distributions; a reasonable presumption is that this design excludes a greater proportion of the poor, the

---

*The unidentified Institute members involved in the undertaking were: Iqbal Alam, Stephen E. Guisinger, Sarfraz K. Qureshi and Abdul Wasay.

*The \( ith+1 \) dwelling address was sampled whenever the \( ith \) dwelling was: (1) unattended during two re-visits, (2) vacant, (3) an establishment, (4) an institution, or (5) government-owned.
illiterate, and the recent migrant, so that the effect—if any—of the sampling error is to underestimate the return to primary education. With respect to other variables (such as age, sex, and occupation), a post-selection examination of the distributions of the sampled labour force members with the corresponding distributions identified by the earlier and larger—311,749 persons—1960 socio-economic survey of Rawalpindi [10], indicates that the two samples are similarly distributed and, to the extent that the earlier survey is representative, the present survey is representative.

Several checks were undertaken to gauge the extent of nonsampling error in the survey; there are two types: response and nonresponse. With regard to response errors, the likelihood of unintentional recall errors is relatively low as all questions pertain to basic, easily recallable information: age, sex, employment status, and the like; however, the self-employed appear to have greater difficulty in interpreting their hours worked than do employees: the former typically work from sunrise to sunset even though they always manage to have meals and an afternoon rest in between! A more serious type of response error is the likelihood of the intentional underreporting of income. To control for this problem, expenditure and type-of-housing questions were asked to determine a lower bound to household income; in addition, the enumerators were asked to note their opinion in each completed questionnaire on the probability of underreporting. A careful analysis of these controls suggests some potential instances of income underreporting; but none of these were particularly unbelievable to justify elimination.

Finally, there is the possibility of nonresponse errors. These errors are usually traceable to improperly completed questionnaires and careless data transcription. The twin procedures adopted to check for these errors are field checks by Institute staff and data editing. Aside from the already noted field checks, approximately 20 percent of the sample households were visited by Institute staff and no instances of enumerator-counterfeited questionnaires for nonexistent households were noted. The data were manually edited at the coding and card punching stages, and computer-edited through multiple consistency checks at the print-out stage: minor errors were spotted and corrected.
## Appendix Table 1

### Annual Educational Expenditure Estimates Per Student by Level

<table>
<thead>
<tr>
<th>Educational level</th>
<th>Years of Schooling</th>
<th>Total</th>
<th>Private</th>
<th>Total</th>
<th>Direct</th>
<th>Government</th>
<th>Indirect</th>
<th>Annual Amortization</th>
<th>Total</th>
<th>Building</th>
<th>Equipment</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>(1)</td>
<td>(2)</td>
<td>(3)</td>
<td>(4)</td>
<td>(5)</td>
<td>(6)</td>
<td>(7)</td>
<td>(8)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>School</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Primary</td>
<td>5</td>
<td>276</td>
<td>30</td>
<td>246</td>
<td>145</td>
<td>101</td>
<td>810</td>
<td>660</td>
<td>150</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Middle</td>
<td>3</td>
<td>547</td>
<td>40</td>
<td>507</td>
<td>300</td>
<td>207</td>
<td>1,666</td>
<td>250</td>
<td>1,416</td>
<td></td>
<td></td>
</tr>
<tr>
<td>High</td>
<td>2</td>
<td>758</td>
<td>48</td>
<td>710</td>
<td>400</td>
<td>310</td>
<td>2,500</td>
<td>500</td>
<td>2,000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>College</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intermediate</td>
<td>2</td>
<td>2,376</td>
<td>445</td>
<td>1,931</td>
<td>1,000</td>
<td>931</td>
<td>7,500</td>
<td>1,000</td>
<td>6,500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Degree</td>
<td>2</td>
<td>2,910</td>
<td>469</td>
<td>2,441</td>
<td>1,200</td>
<td>1,241</td>
<td>10,000</td>
<td>1,500</td>
<td>8,500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>University</td>
<td>2</td>
<td>18,183</td>
<td>769</td>
<td>17,414</td>
<td>5,000</td>
<td>12,414</td>
<td>100,000</td>
<td>15,000</td>
<td>85,000</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Source

### Note
Student residence fees are included in column 2 for the college and university levels. Column 5 is column 6 weighted by an amortization factor, $K/(K-1)$, where $K = (1+r)^t$, $r$ = a rate of discount, and $t$ = the expected life of building and equipment in years; $r$ is set at 12 percent and $t$ is set at 30.
References


